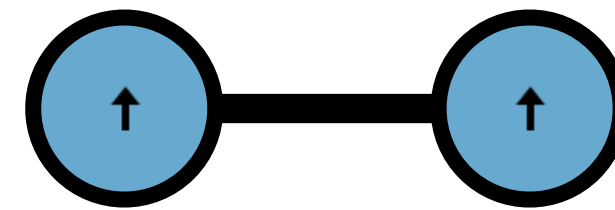
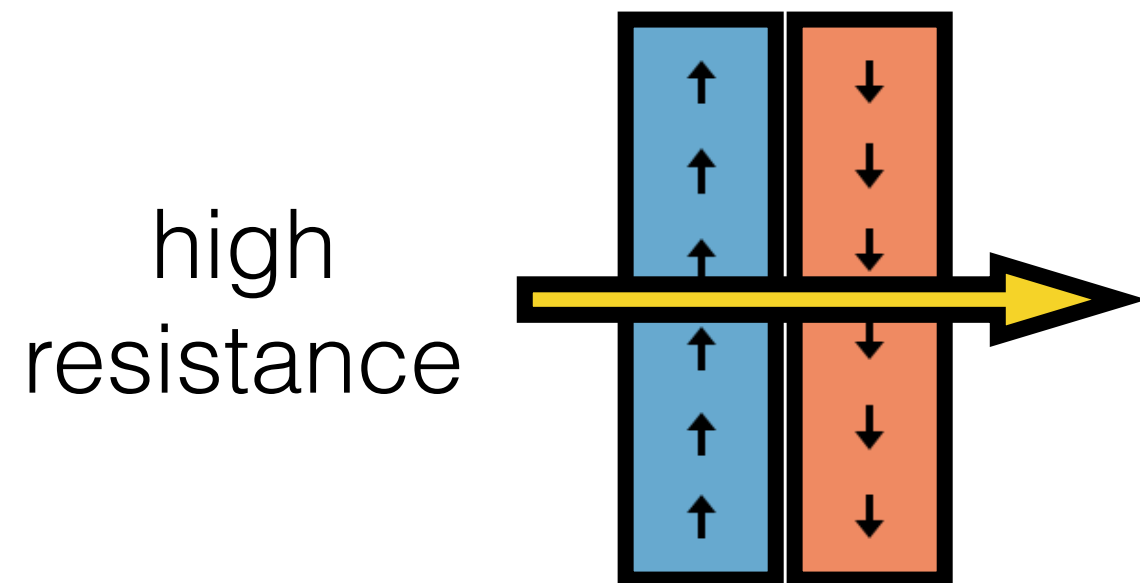
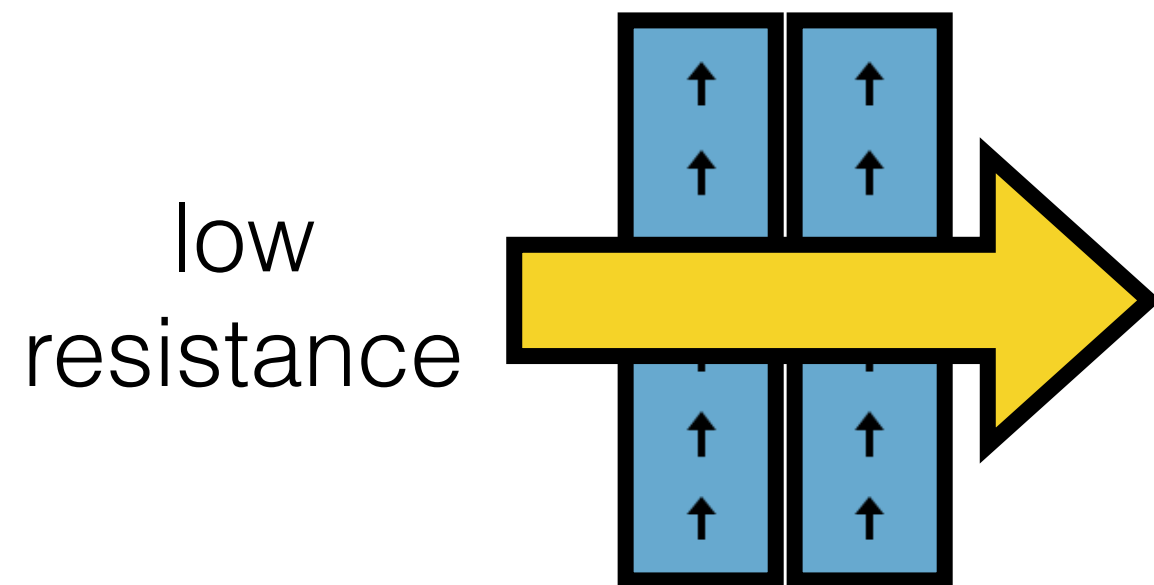


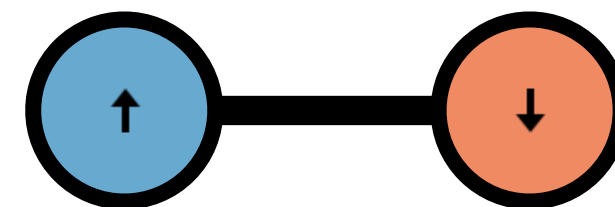
Theoretical investigation of magnetic exchange interactions in dilute magnetic semiconductor quantum dots induced by defects

Joshua Goings and Xiaosong Li
Tuesday, December 15, 11:20am

Controlling magnetism at the nanoscale is important.



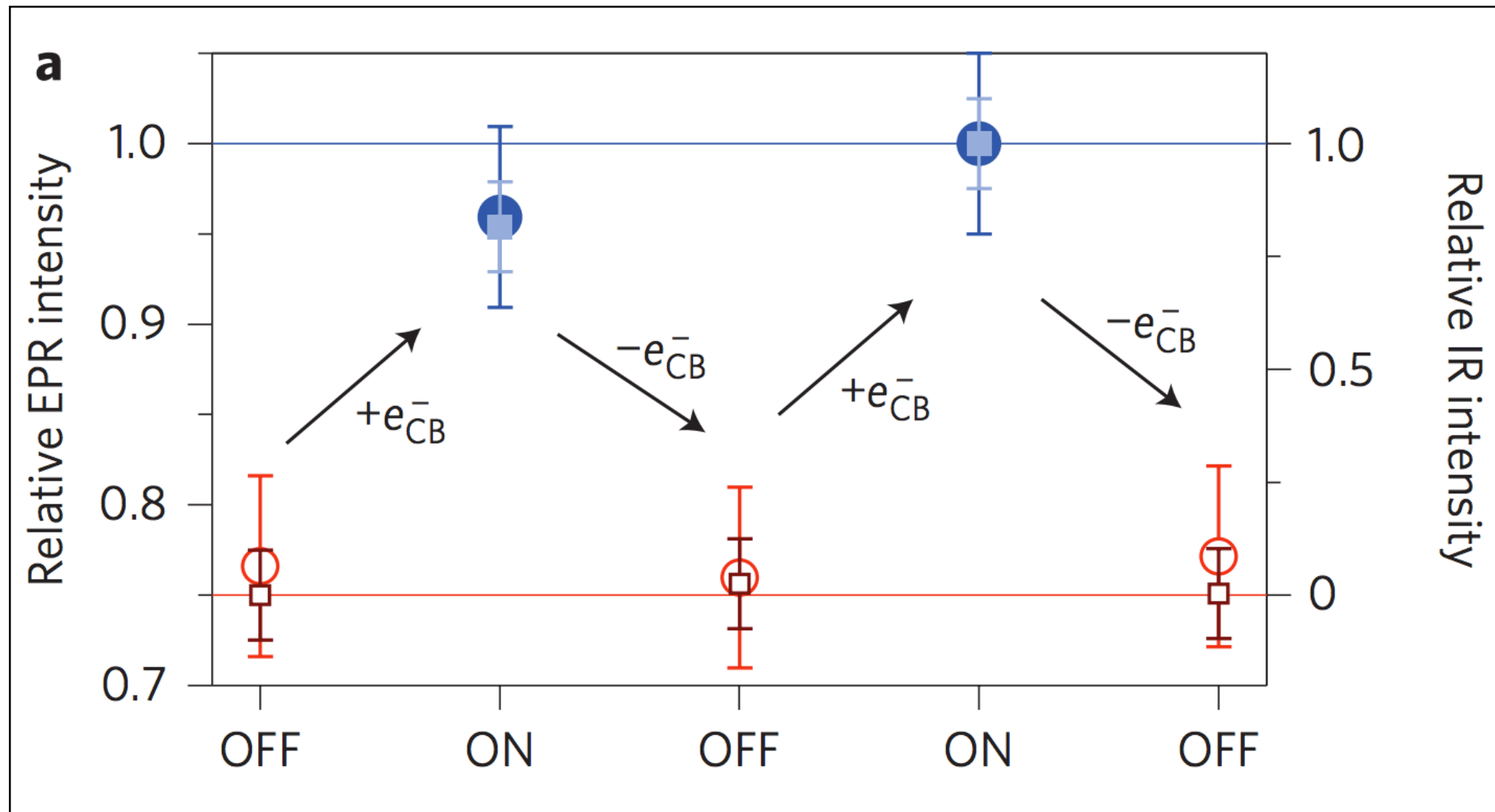
ultimate miniaturization:
ferromagnetic quantum dots linked
by semiconducting polymer



Tunnel Magnetoresistance
(TMR)

Mn²⁺:ZnO Nanocrystals (NC)

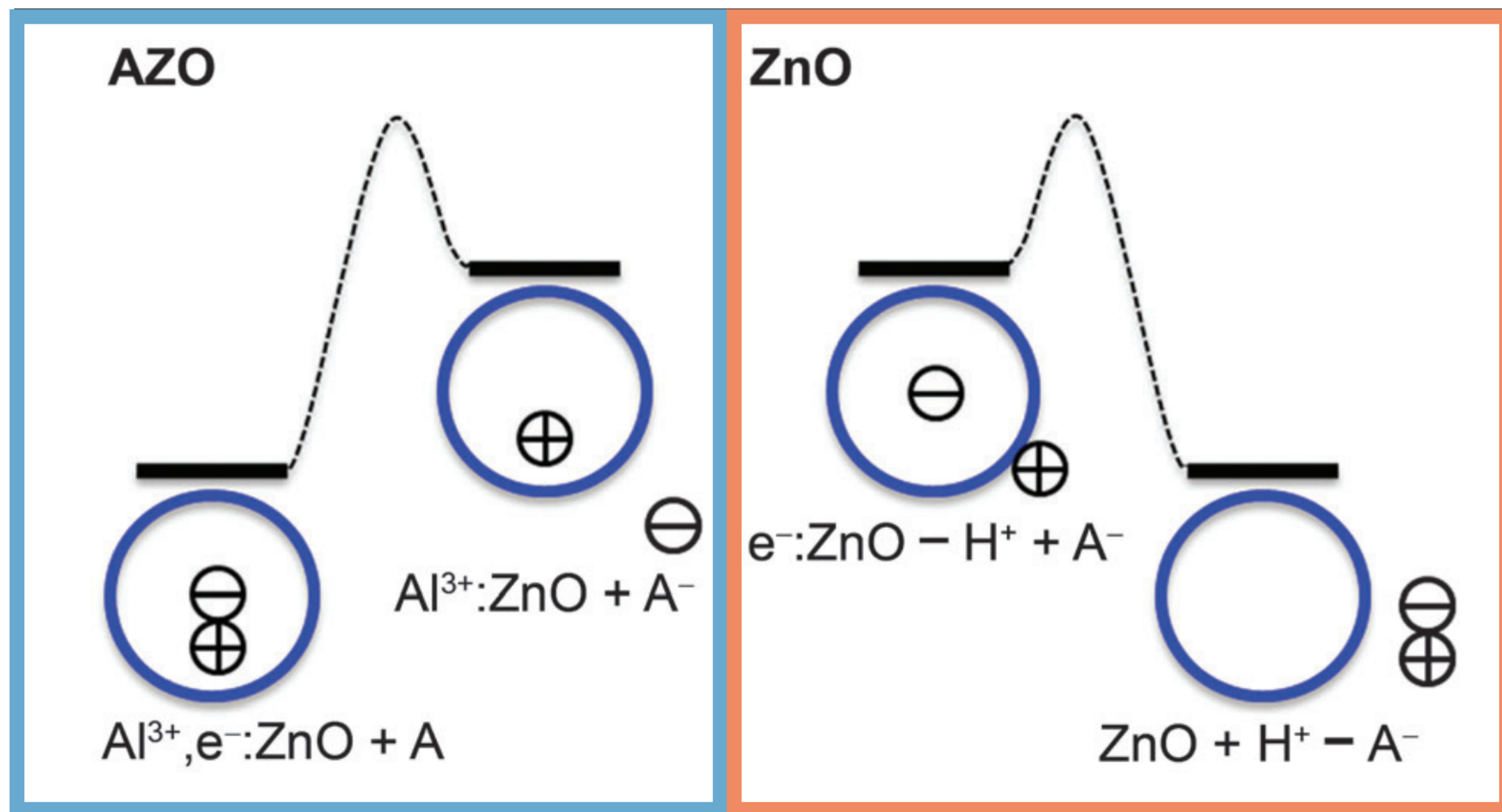
Adding charge carriers can induce magnetic response



Oschenbein, *et al.* Nature Nanotechnology 4, 681 - 687 (2009)

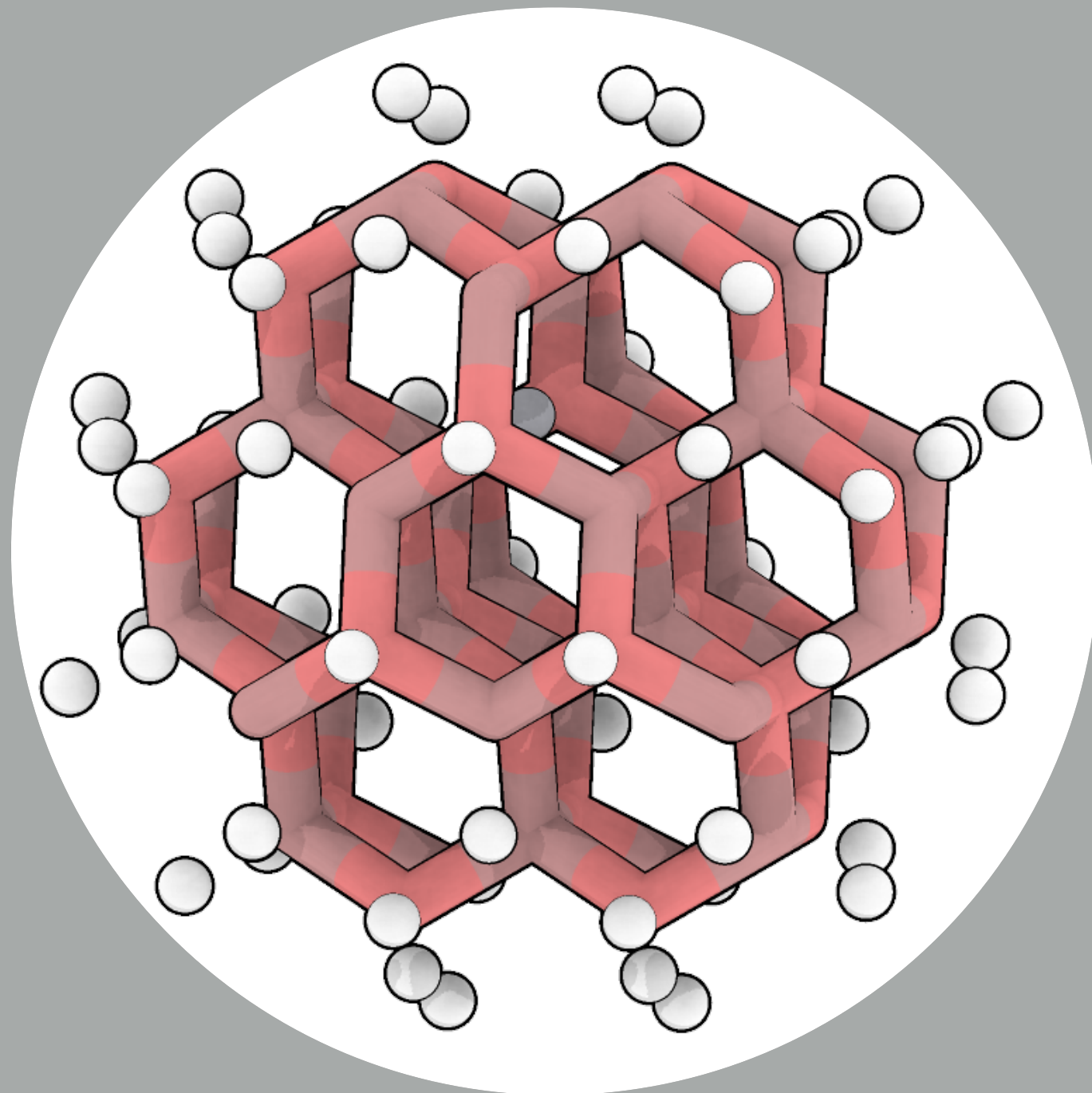
Al³⁺-doping ZnO:

a stable way to add electrons to a ZnO nanocrystal.



Can we create permanent ferromagnetic QDs by co-doping (Al,Mn)-ZnO?

Is Al-doped MnZnO fundamentally any different than electronically doped MnZnO?

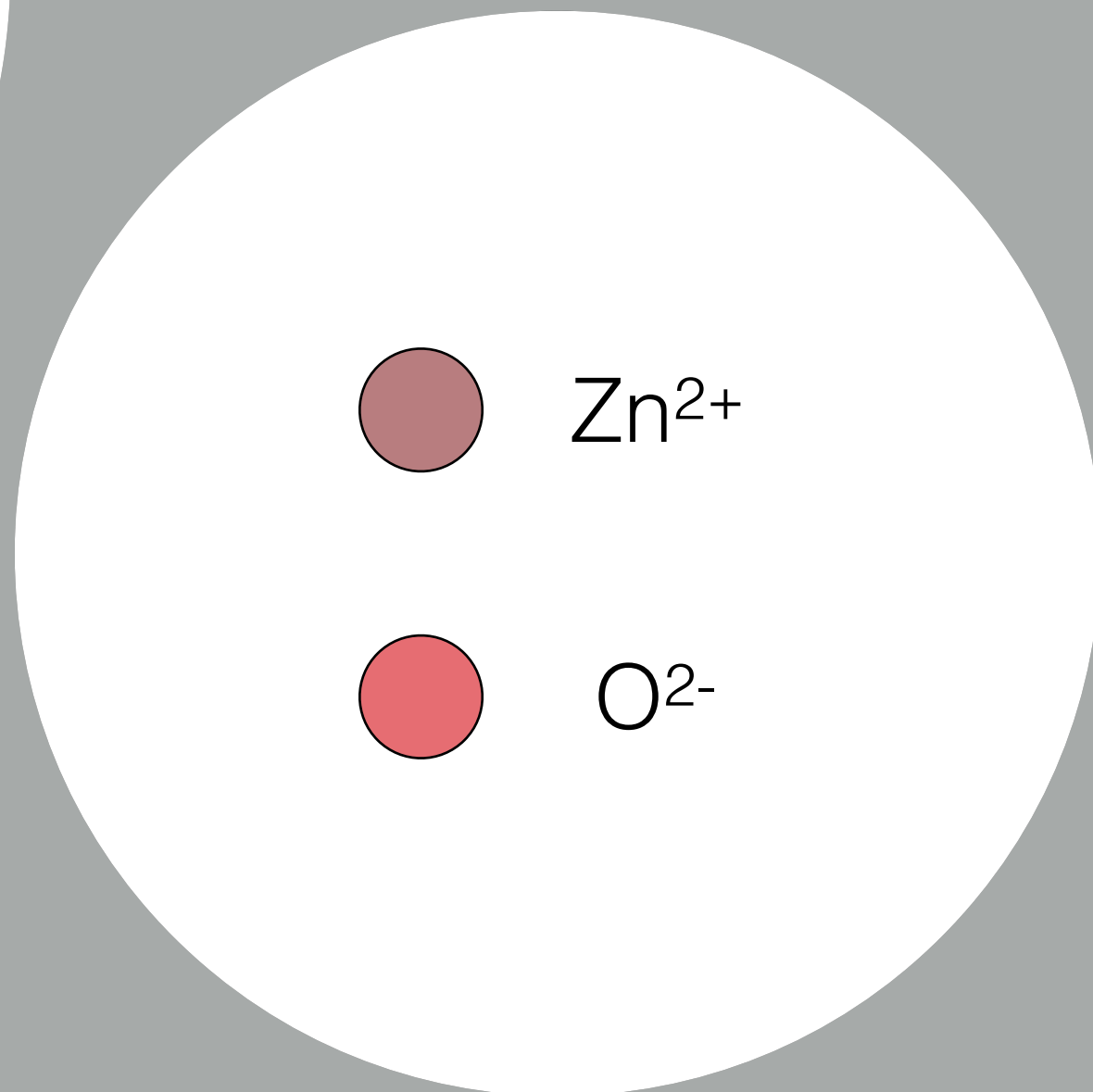
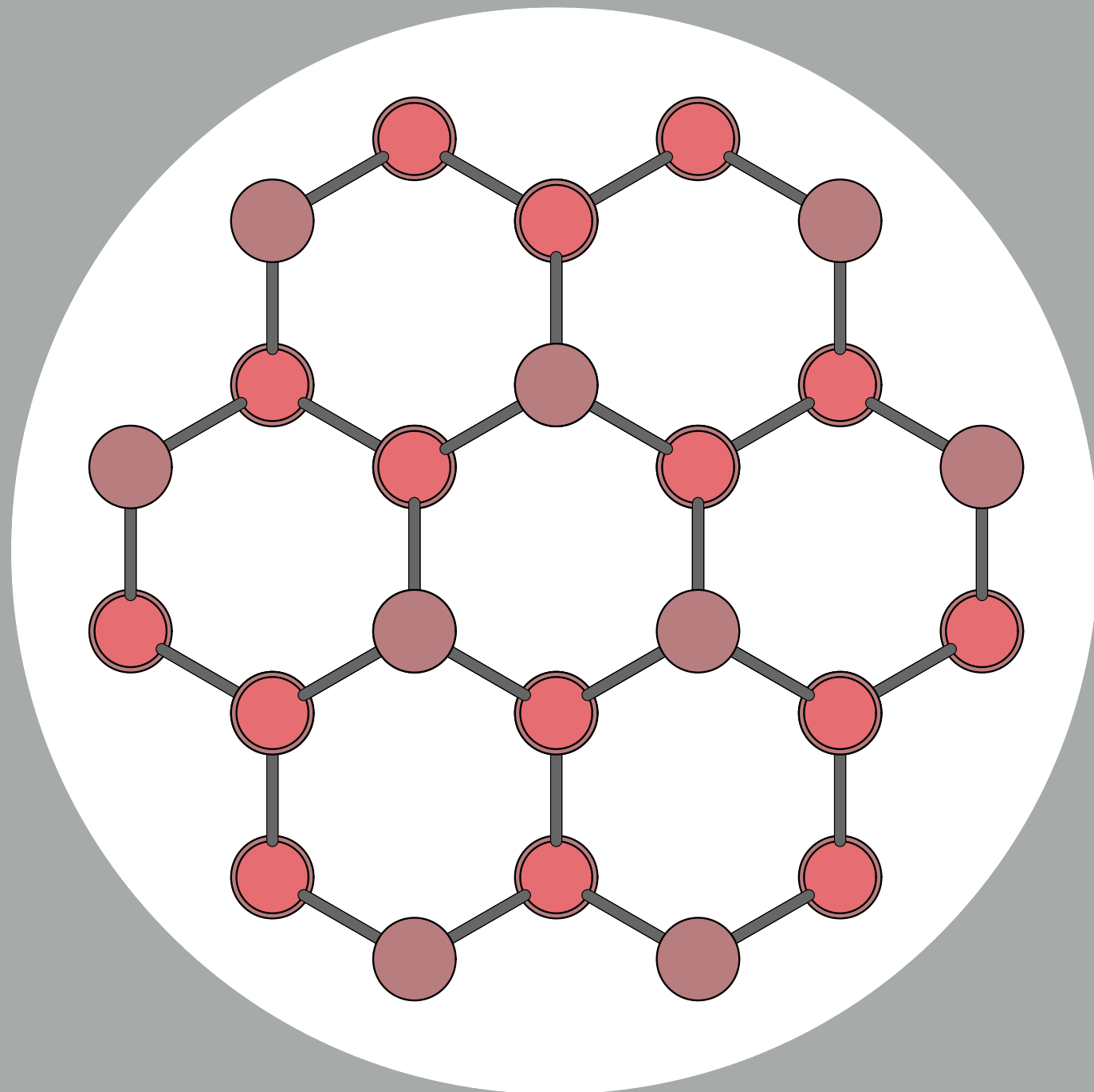


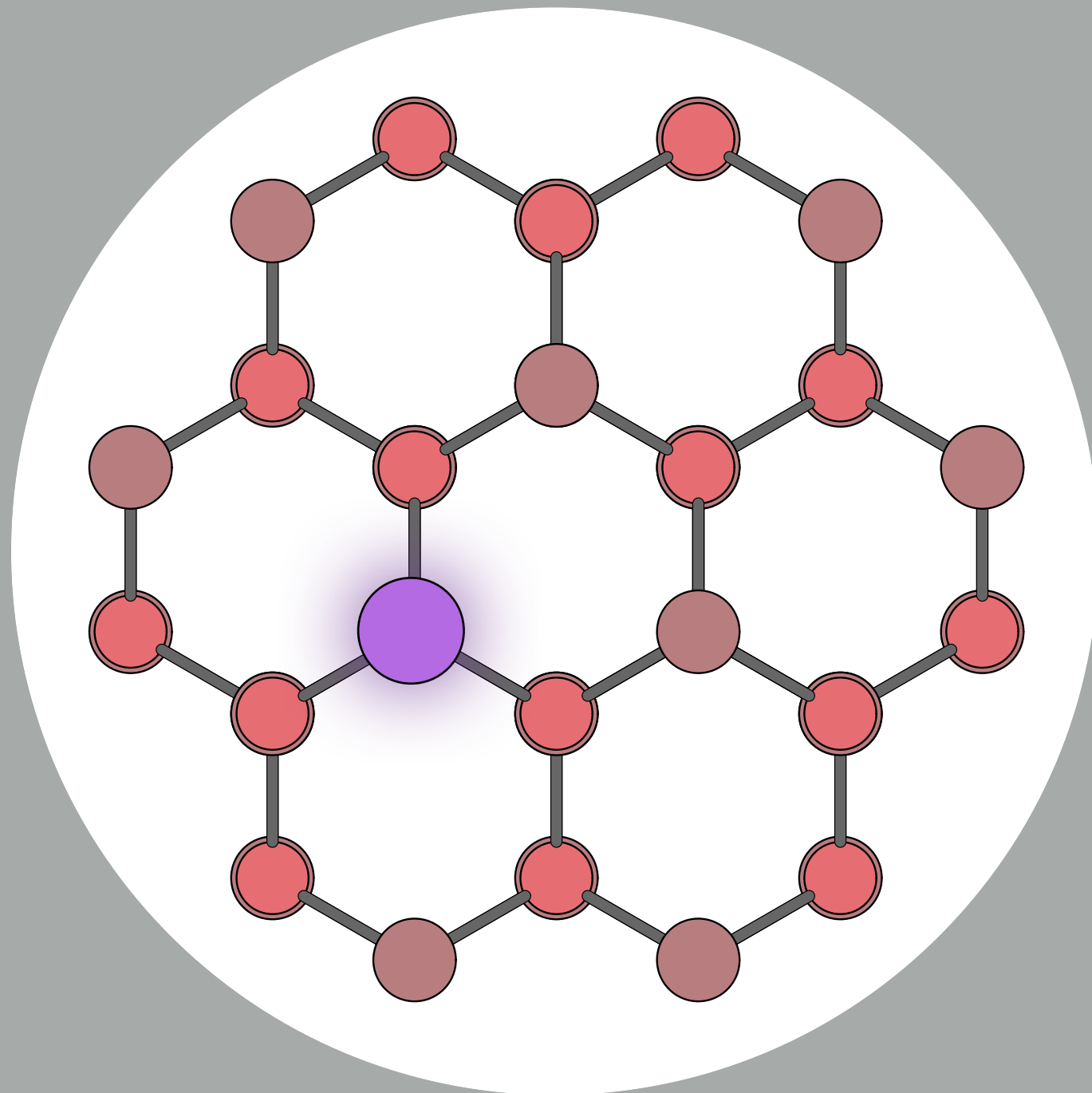
model ZnO

1.3 nm diameter

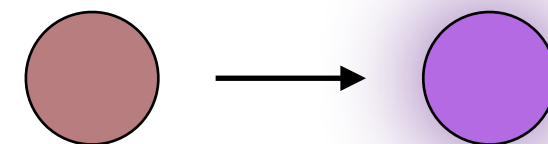
PBE1PBE/LANL2DZ

pseudohydrogen
capping

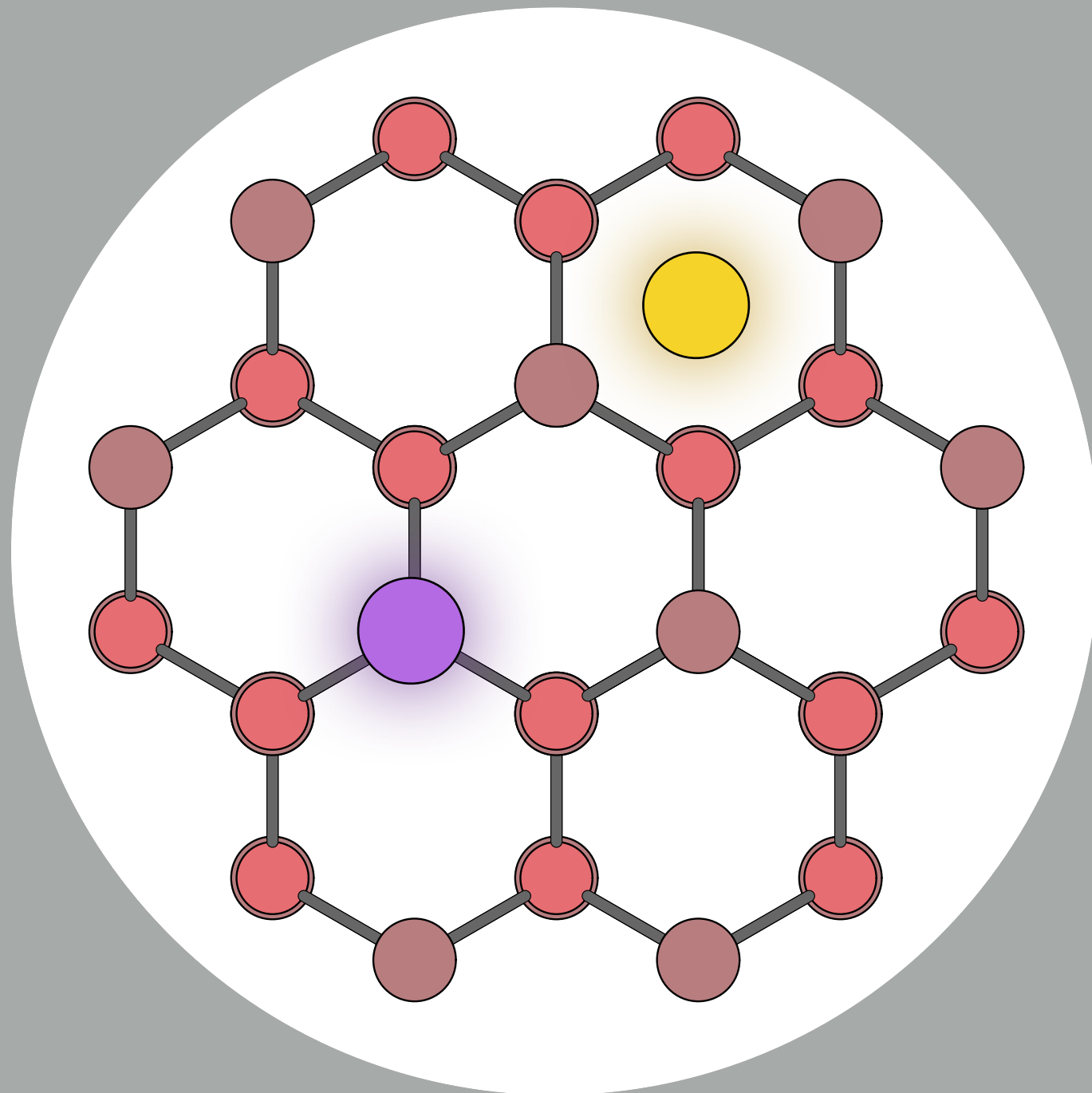




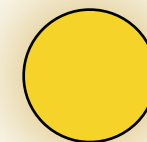
Replace Zn^{2+} with Mn^{2+}



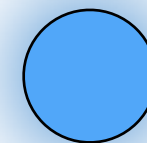
$$S = 5/2$$



Add charge carrier



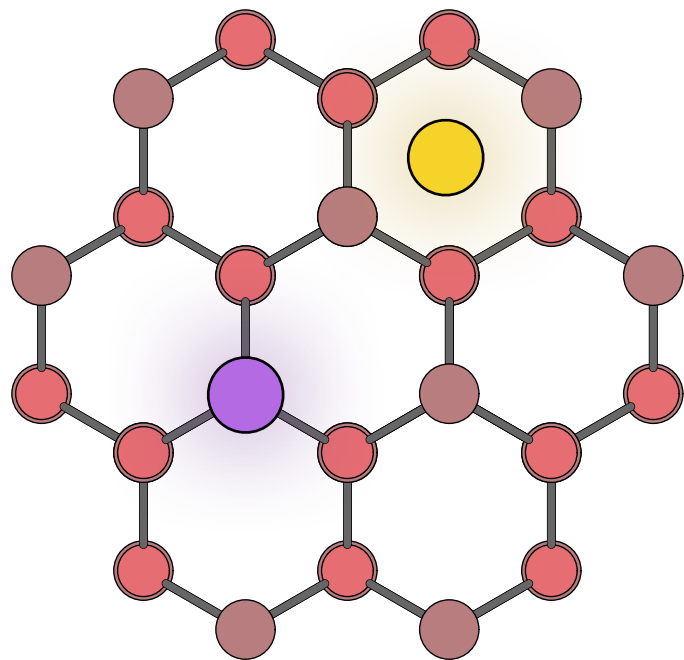
electron



hole

$$S = 1/2$$

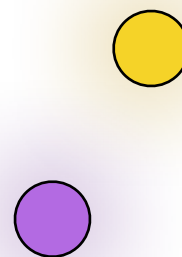
$$\hat{H}_{exact}$$



unparameterized;
all interactions

Map DFT to
spin Hamiltonian

$$\hat{H}_{HDVV}$$

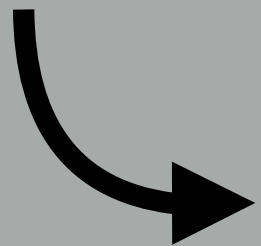


$$-2J\hat{S}_i\hat{S}_j$$

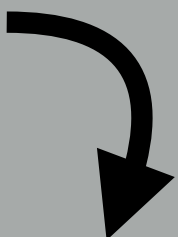
only spin
interactions

Map DFT to spin Hamiltonian

H_{eff} = Energy difference of DFT spin configurations



Plug in spin of
local spin subsystem



$$H_{\text{eff}} = J[S_i(S_i + 1) + S_j(S_j + 1) - S_{i+j}(S_{i+j} + 1)]$$



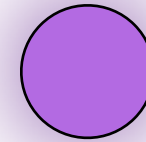
Solve for J

*more details at end

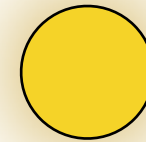
Two-center spin interactions:

charge-doped MnZnO quantum dots

Mn²⁺



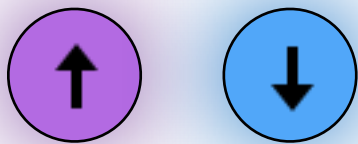
electron



hole



h⁺



$$J_{\text{p-d}} = -152 \text{ meV}$$

anti-ferromagnetic (AFM)

e⁻



$$J_{\text{s-sd}} = +11 \text{ meV}$$

ferromagnetic (FM)

A³⁺

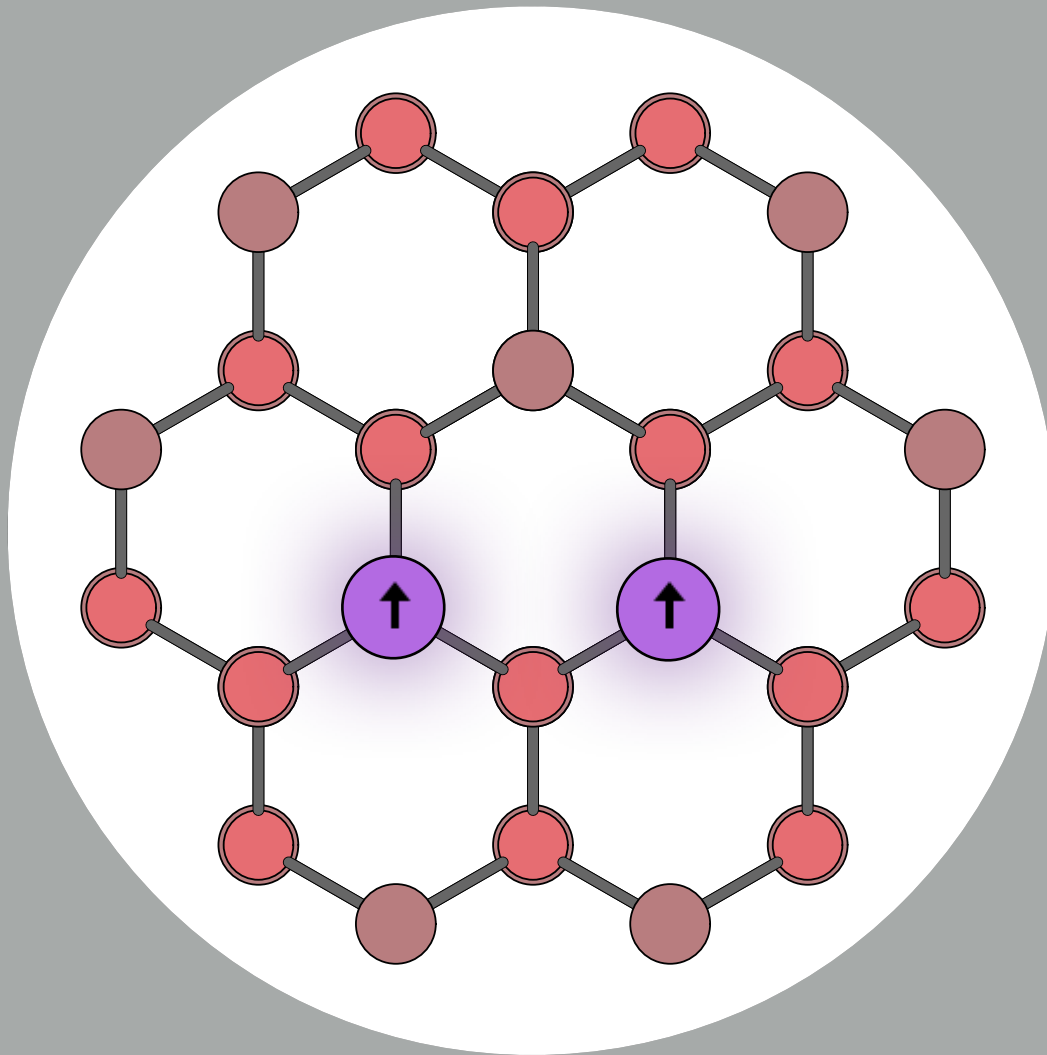


$$J_{\text{s-sd}} = +9 \text{ meV}$$

ferromagnetic (FM)

$$J > 0 \rightarrow \text{FM}, \quad J < 0 \rightarrow \text{AFM}$$

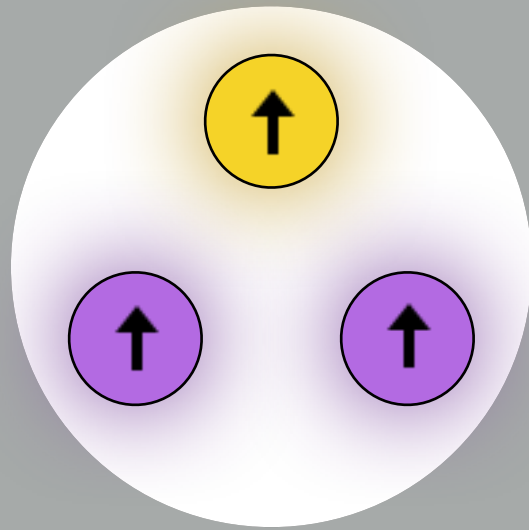
Nearest neighbor $\text{Mn}^{2+} - \text{Mn}^{2+}$
anti-ferromagnetic (AFM)
super exchange (SE) interactions



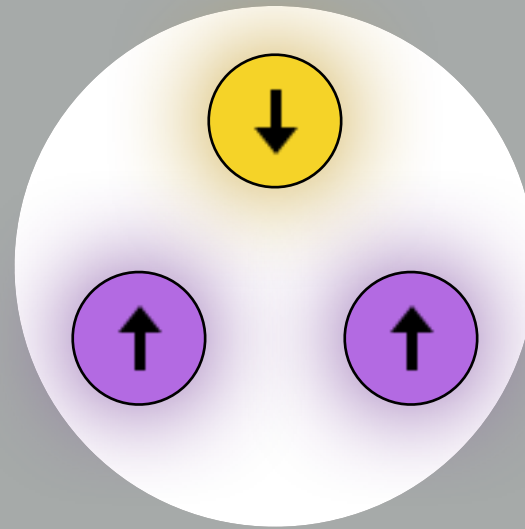
$$J_{\text{SE}} = -2.4 \text{ meV}$$

Subsequent interaction with charge carrier
leads to spin frustrated interactions

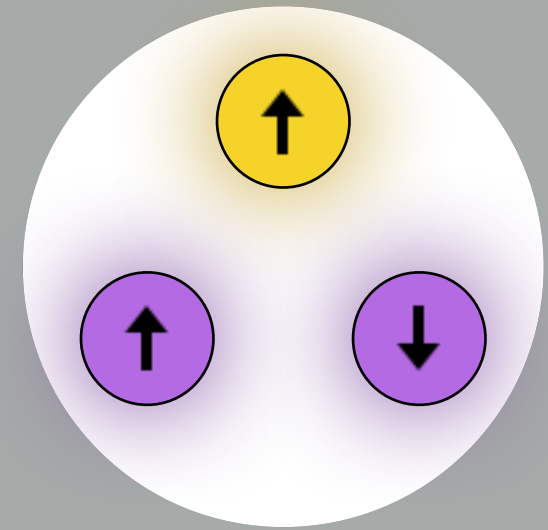
Gives rise to three possible spin configurations



High-spin
(HS)

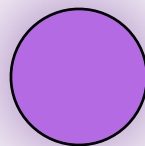


ferromagnetic
(FM)

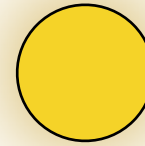


anti-ferromagnetic
(AFM)

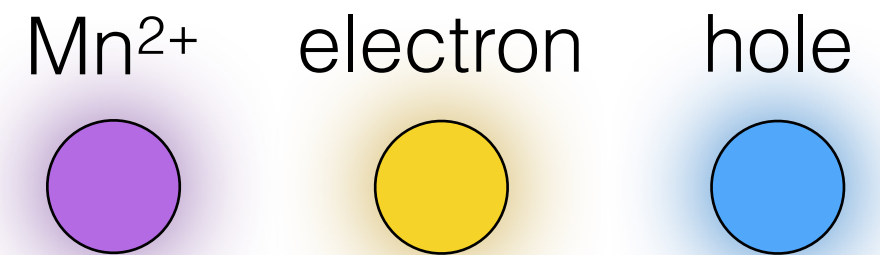
Mn²⁺



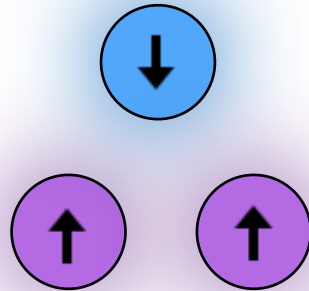
charge-carrier



Three-center spin interactions: charge-doped MnZnO quantum dots



h⁺

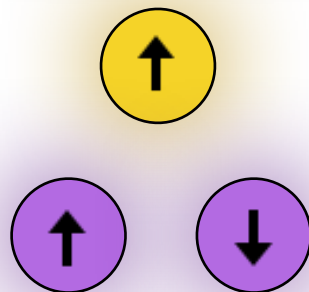


$$J_{\text{SE}} = -13 \text{ meV}$$

$$J_{\text{p-d}} = -127 \text{ meV}$$

ferromagnetic
(FM)

e⁻

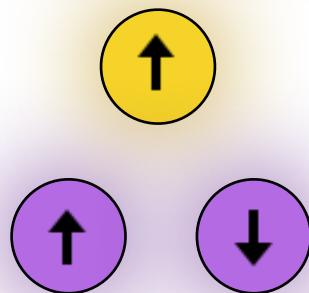


$$J_{\text{SE}} = -2 \text{ meV}$$

$$J_{\text{s-sd}} = +11 \text{ meV}$$

anti-ferromagnetic
(AFM)

Al³⁺



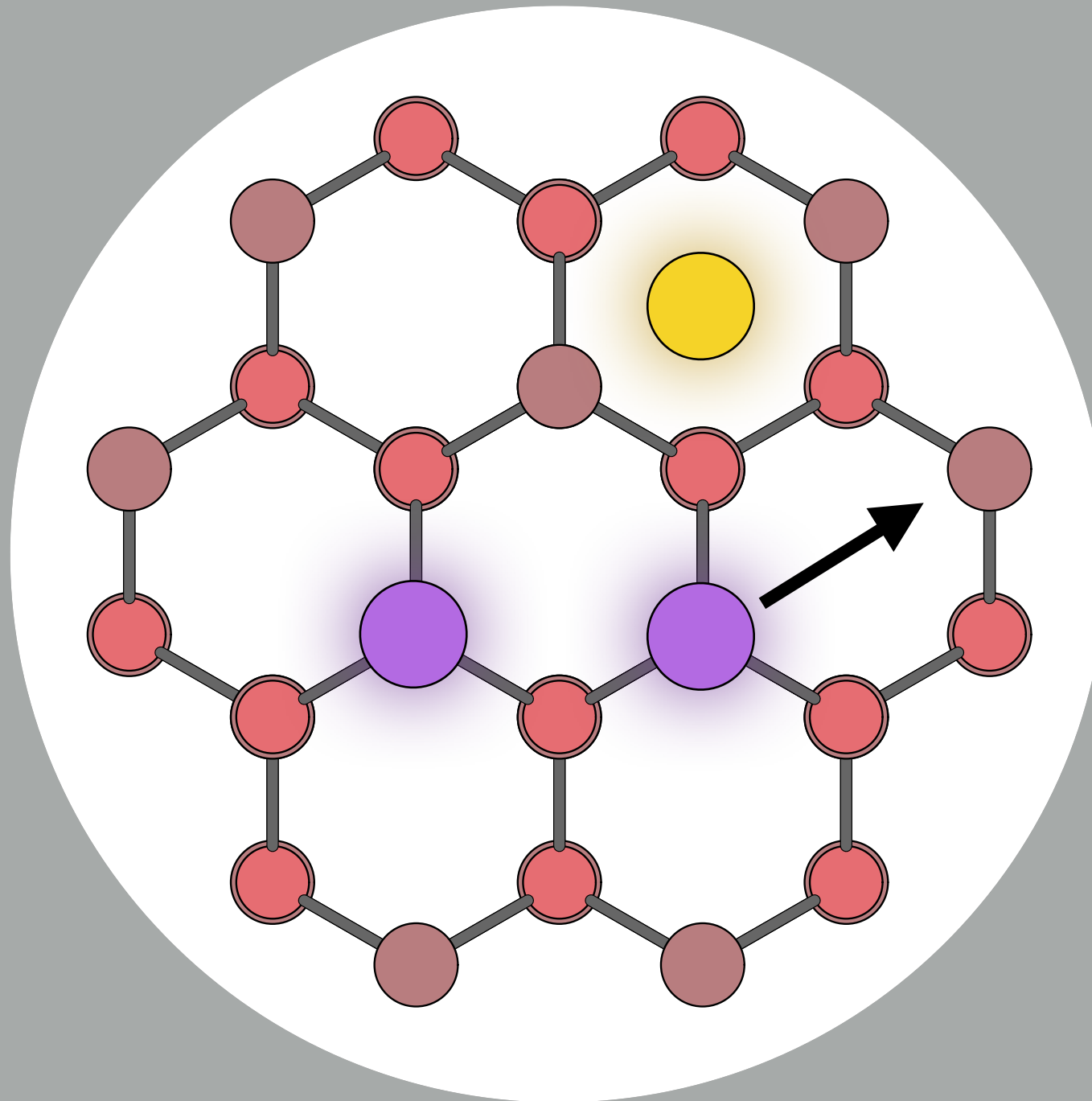
$$J_{\text{SE}} = -2 \text{ meV}$$

$$J_{\text{s-sd}} = +9 \text{ meV}$$

anti-ferromagnetic
(AFM)

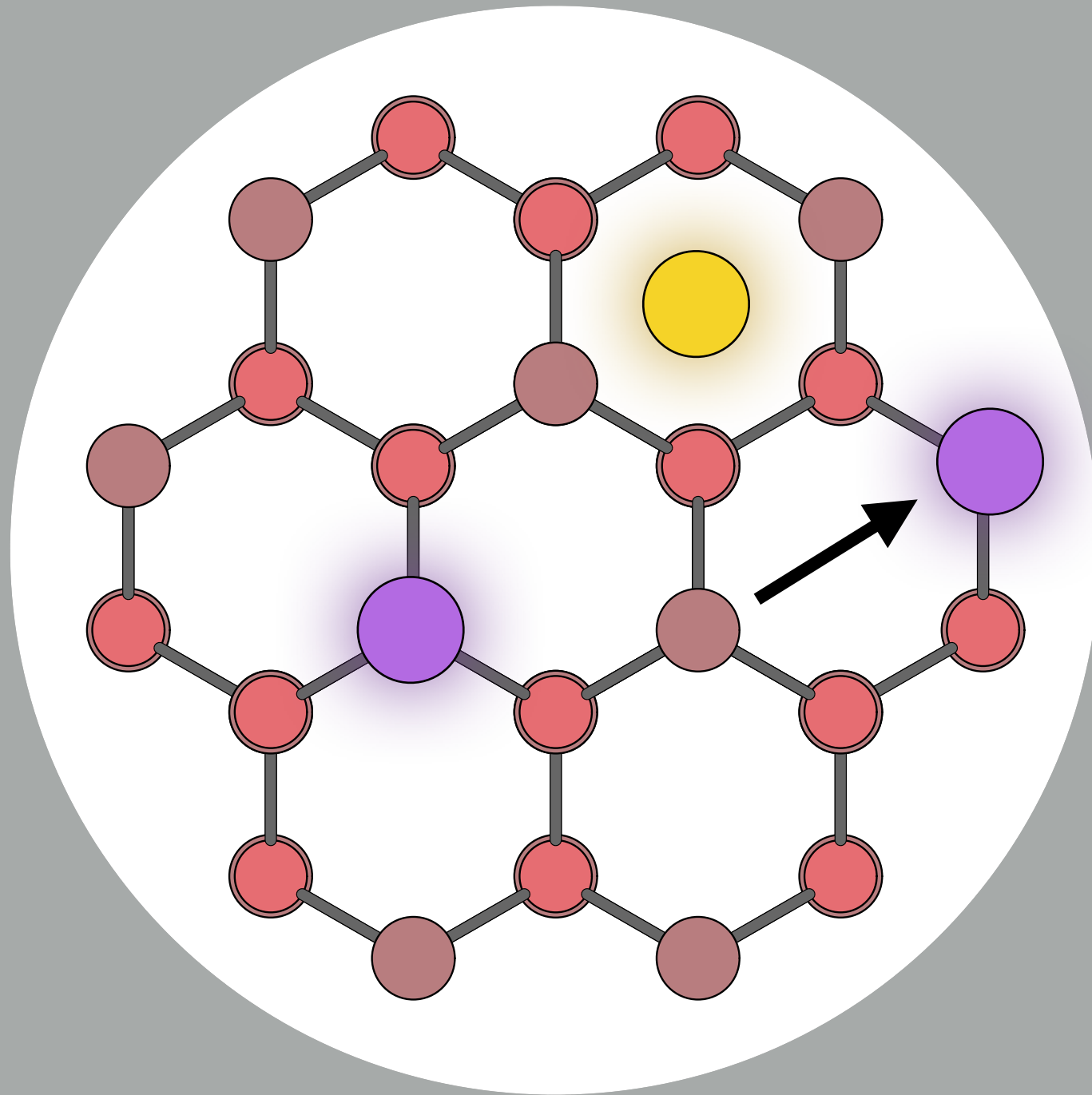
Spins compete, and FM favored when $5J_{\text{SE}} > J_{\text{carrier-Mn}}$

Of course, the interaction is highly position dependent.



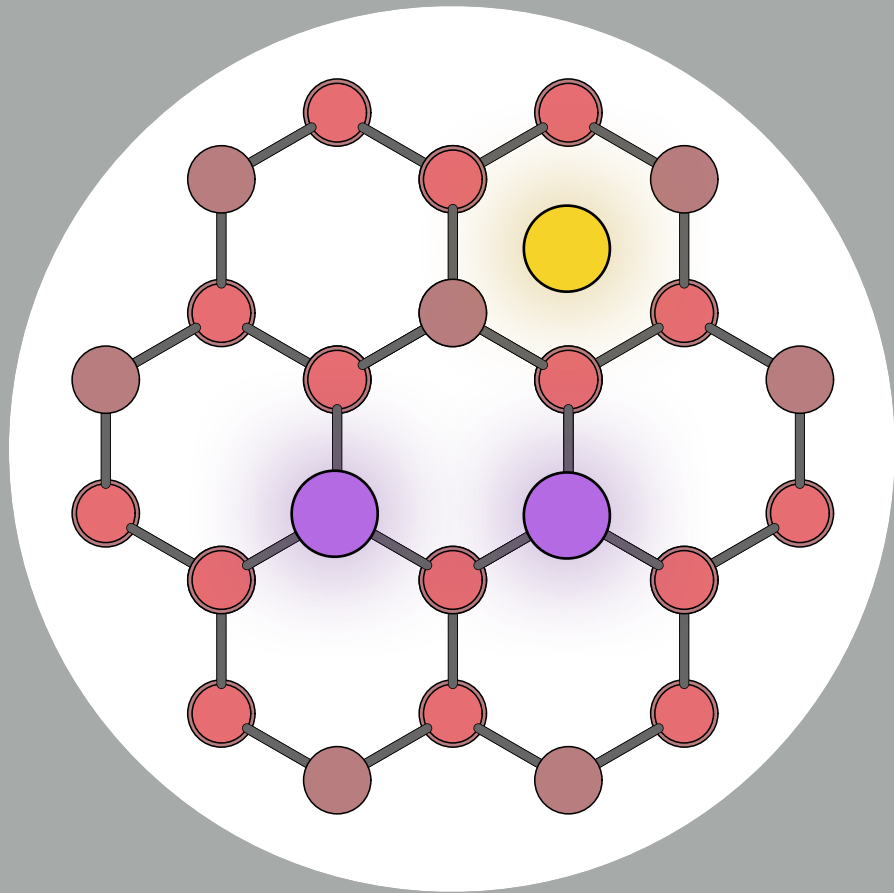
Split up Mn dimer, lose SE interactions, FM favored again.

Of course, the interaction is highly position dependent.



Split up Mn dimer, lose SE interactions, FM favored again.

(Mn,Al) co-doped ZnO quantum dots



Aluminum-doping leads
to stable charge carrier

Charge can mediate ferromagnetic
spin coupling between distant Mn
centers

Thank you!



Map DFT to spin Hamiltonian

$$H_{\text{eff}} = \Delta E = E(\text{DFT spin config 1}) - E(\text{DFT spin config 2})$$

$$H_{\text{eff}} = -2J \hat{S}_i \cdot \hat{S}_j$$

$$-2\hat{S}_i \cdot \hat{S}_j = \hat{S}_i^2 + \hat{S}_j^2 - (\hat{S}_i + \hat{S}_j)^2 \quad \text{complete the square}$$

$$\hat{S}_i^2 |\psi\rangle = S_i(S_i + 1) |\psi\rangle \quad \text{act on spin eigenfunction}$$

This gives for spin subsystems (i) and (j) :

$$H_{\text{eff}} = J[S_i(S_i + 1) + S_j(S_j + 1) - S_{i+j}(S_{i+j} + 1)]$$